

Population Aging, Skill-Composition, and Technology Adoption

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Introduction

- ▶ The **workforce is aging** in most developed economies.
 - **Share 45+** in US: ↑ from 38.5% in 2004 to 42%, and to 44.5% by 2034. [BLS]
- ▶ Aging affects the **skill-mix** of the workforce
 - **Older** workers bring more **experience** accumulated on the job. [Ben-Porath, 1967]
 - **Younger** workers bring more **up-to-date skills** [Deming and Noray, 2020]

Introduction

- ▶ The **workforce is aging** in most developed economies.
 - **Share 45+** in US: ↑ from 38.5% in 2004 to 42%, and to 44.5% by 2034. [BLS]
- ▶ Aging affects the **skill-mix** of the workforce ...
- ▶ ... And generates a **trade-off** for aggregate productivity
 - **Old workers** ↑ \implies experience ↑ \implies **Productivity** ↑.
 - **Young workers** ↓ \implies tech-skills ↓ \implies **Technology Adoption** ↓ \implies **Productivity** ↓
- ▶ Net effect is **ex-ante ambiguous** and depend on multiple factors
 - e.g., complementarity b/w skills, speed of tech progress, cost of retraining.
- Q. What is the impact of population aging on **aggregate labor productivity**?

Related Literature

▶ Effect of population aging on firm dynamics and TFP.

Maestas et al. [2023], Aksoy et al. [2019], Hopenhayn et al. [2022], Bloom et al. [2020], Karahan et al. [2024], Angelini [2023], Inokuma and Sanchez [2023], Peters and Walsh [2021]

- Our Paper: Aging change the workforce composition, not only the size of labor force.

▶ Vintage human capital and technology diffusion.

Chari and Hopenhayn [1991], MacDonal and Weisbach [2004], Adão et al. [2024], Violante [2002]

- Our Paper: Multi-dimensional skills that are portable across technologies.

▶ Workers Age and New Technologies

Lipowski [2024], Deng et al. [2024], Deming and Noray [2020], Acemoglu and Restrepo [2022]

- Our Paper: Young workers are an important input for technology adoption of firms.

Today's Talk

Empirics: Show that **young workers** have a **comparative advantage** in new technologies.

- ▶ Firms with Younger workforce: Prob. Adopt Tech \uparrow .
- ▶ Young workers: Prob. tech-related tasks \uparrow + Productivity Gains from Adoption.
- ▶ Adoption tilts workforce toward young workers.

Theory: Model with firm dynamics + labor market frictions + multi-dimensional skills.

- ▶ **Experience** + **Tech-Skills**: evolve over workers career.
- ▶ Firms choose between **frontier** and **laggard** technology.
- ▶ Frontier technology is **tech-skill intensive**.

Q. Decompose the impact of population aging on aggregate labor productivity.

- ▶ Technology Adoption + Matching Frictions under skill-scarcity.

Outline

1. Empirical Analysis
2. The Model
3. Productivity and Misallocation

Data

Main Goal: Link firm-level tech adoption to info on workforce composition.

German Admin Data: Matched Employer Employee + Tech Adoption Surveys.

▶ **Linked Employer-Employee (1993-2021)**

- **Firms**: Workforce Composition, Investment, On-the-job training.
- **Workers**: Wage, Occupations, Unempl. Spells, Education, Demographics.

▶ **LPP (2015, 2019, 2021): Survey of ICT adoption**

- **Digital**: e.g., IoT, Big Data Analytics, AI, Virtual Reality.
- **Automation**: e.g., Robots, Drones, Additive Manufacturing.

Tech Adoption: At least one technology adopted in the last two years.

[LPP Details](#)

Workforce Composition and Tech Adoption

Q. Are firms with a **younger workforce** more likely to adopt advanced tech?

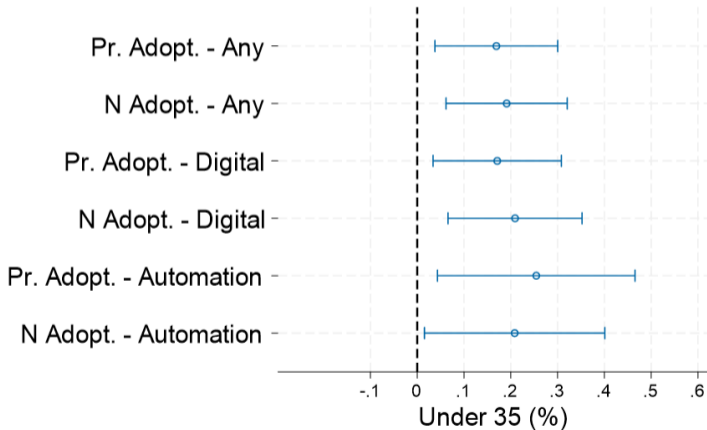
Empirical Specification

$$\mathbb{I}(\text{Adopt})_t = \alpha + \beta \text{ Under 35 (\%)}_{t-1} + \Gamma X_{t-1} + \varepsilon_t$$

- ▶ **Baseline Controls** (X_{t-1}): Firm Size, Firm age, Avg. Wage, College (%), Hiring Rate, Type of Owner.
- ▶ **Fixed Effects**: Sector 3-digit, State, Year, # Tech already used.

Young Workforce Predicts Higher Adoption

- ▶ Moving Up by 1-SD of distribution of U35 % \implies Pr. Adopt \uparrow by 20%.
 \implies # Adoption \uparrow by 20%.



Tasks and Tech Effect on Workers

Q1. Are **younger workers** more likely to carry out **tech-related tasks**?

Q2. How do new technologies affect workers' tasks and productivity?

Empirical Specification

$$\mathbb{I}(Y_{it}) = \alpha + \beta \text{Age}_{it} + \Gamma X_{it} + \underbrace{\gamma f(it)}_{\text{Firm FE}} + \varepsilon_{it}$$

► Outcomes (Y_{it})

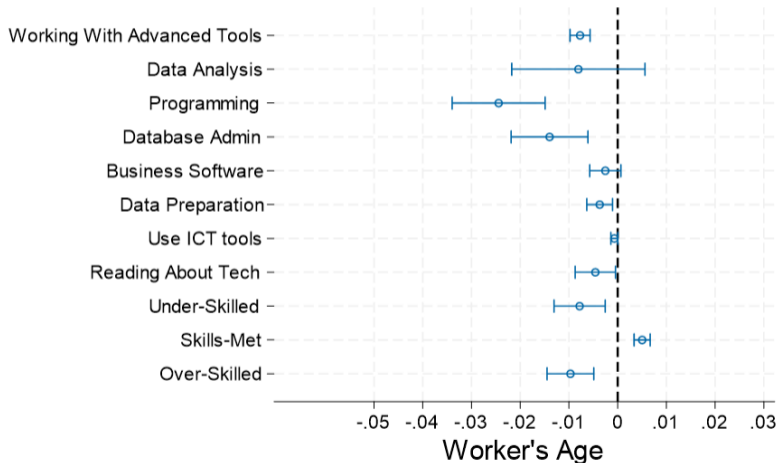
- Task-Related Questions
- Impact of Tech

► Baseline Controls (X_{it}): Wage, Occupation Tenure, Firm Age.

► Fixed Effects: Firm, Year, Task Complexity, College, Occupation (3-digit)

Young Perform More Tech-Related Tasks

► Coefficient: 1 year more \iff Pr. Answer Yes.



Young Report Productivity Gains for Tech Adoption

► Coefficient: 1 year more \iff Pr. Answer Yes.



Event Study Around Adoption

Q. How does firms' **employment** and **workforce composition** change after adoption?

Empirical Strategy

- ▶ Compare dynamic outcomes of **adopting** vs **non-adopting** establishments.

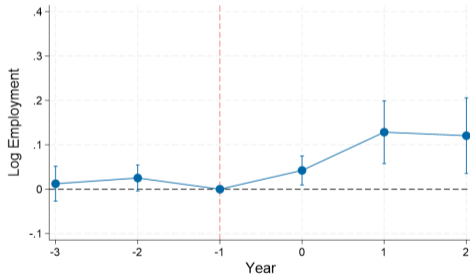
Empirical Specification

$$y_{ft} = \alpha_f + \gamma_t + \sum_k \underbrace{\theta_k D_{ft}^k}_{\text{Non-Adopters}} + \sum_k \underbrace{\beta_k (D_{ft}^k \times \text{Tech Adoption}_f)}_{\text{Adopters}} + \varepsilon_{ft},$$

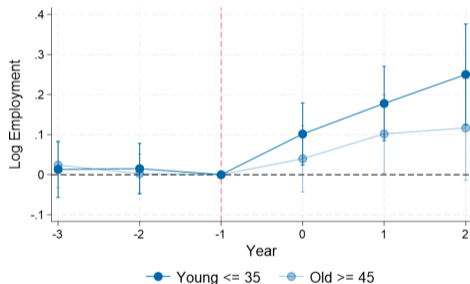
- ▶ **Outcomes** (y_{ft}): Log-Employment, Empl. Composition, Empl. Shares, Wages
- ▶ **Fixed Effects**: Establishment, Sector 3-digit, State, Year.

Event Study - Employment

- ▶ Firms expand employment primarily by hiring young.



(a) Log Employment



(b) Age Heterogeneity

Empl. Share

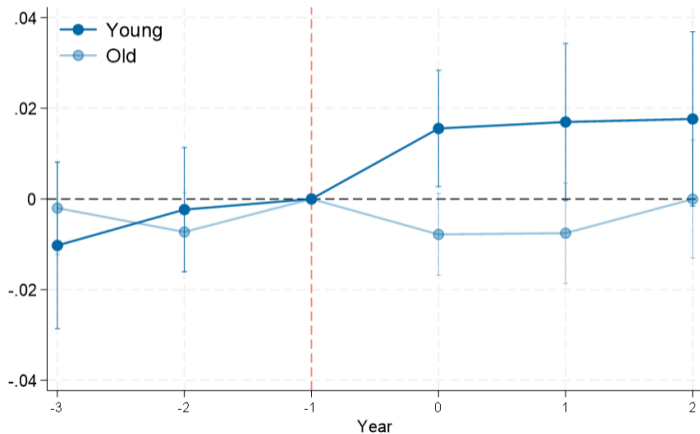
Under 40

College

Automation Tech

Event Study - Incumbent Workers

- ▶ Young Incumbents enjoy higher earnings \implies Productivity Gains.



Outline

1. Empirical Analysis
2. The Model
3. Productivity and Misallocation

Overview of the Model

▶ Model Ingredients

1. Firm Dynamics + Endogenous Technology Adoption.
2. Workers are heterogeneous in **Tech-Skills** and **Experience**.
3. Workforce is a state variable for the firms → Frictional Labor Market.
 - ▶ Directed Search from Unemployment.

▶ Purpose of the Model

1. **Decompose** impact of population aging on productivity into **multiple-channels**
 - ▶ Technology Adoption.
 - ▶ Firm Dynamics + Allocation of workers to firms via search frictions.
2. **Policy Counterfactuals**: e.g., subsidy to on-the-job training / changing firing costs.

Agents

Multi-worker firms

State variables: (\vec{n}, τ, z)

- ▶ Workforce Composition
- ▶ Technological Level: Endogenous
- ▶ Idiosyncratic Productivity: Exogenous

Choose:

- ▶ Technology investment (a)
- ▶ Hiring market and effort (v, W)
- ▶ Employees' long-term contract (\mathcal{C})

Workers

State variables:

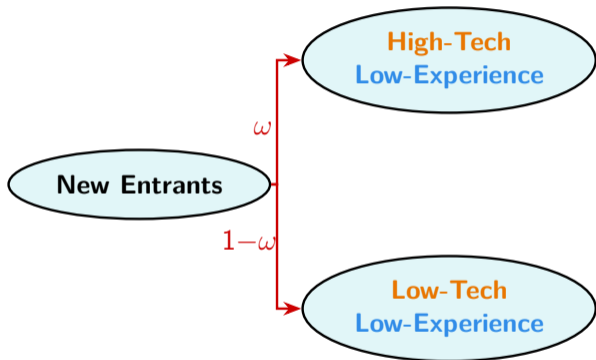
- ▶ Tech skills, H/L: $s_T \in \{\gamma_T^H, \gamma_T^L\}$
- ▶ Experience, H/L: $s_E \in \{\gamma_E^H, \gamma_E^L\}$

\implies Four types: $s \in \mathcal{S} \equiv \{LL, LH, HL, HH\}$

Choose:

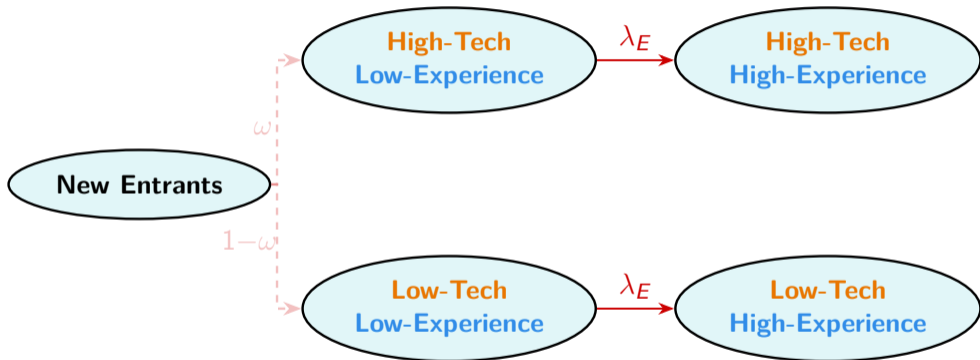
- ▶ Hiring market, when unemployed

Workers: Skill Transitions



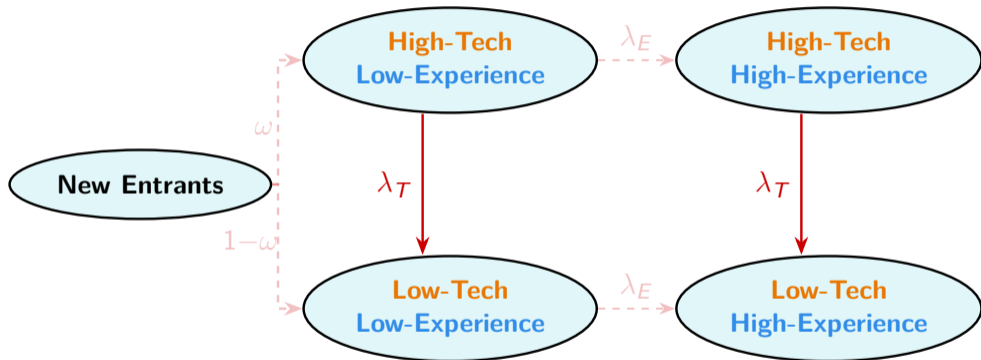
- ▶ A share ω of new workers start with **High-Tech**, all have **Low-Experience**

Workers: Skill Transitions



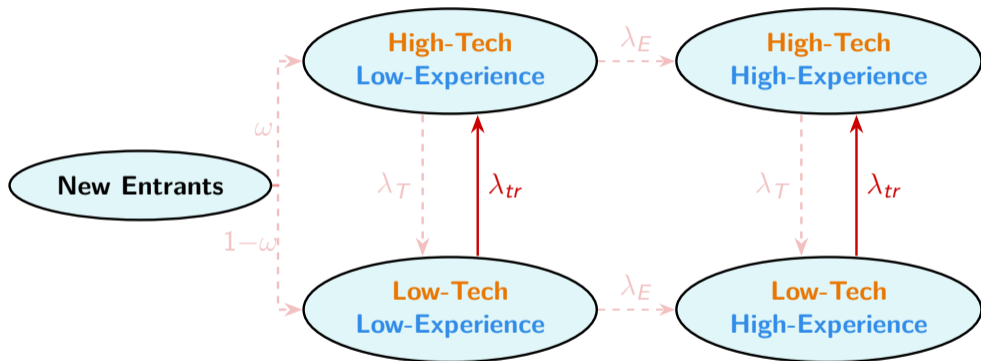
- ▶ Workers accumulate experience at rate λ_E .

Workers: Skill Transitions



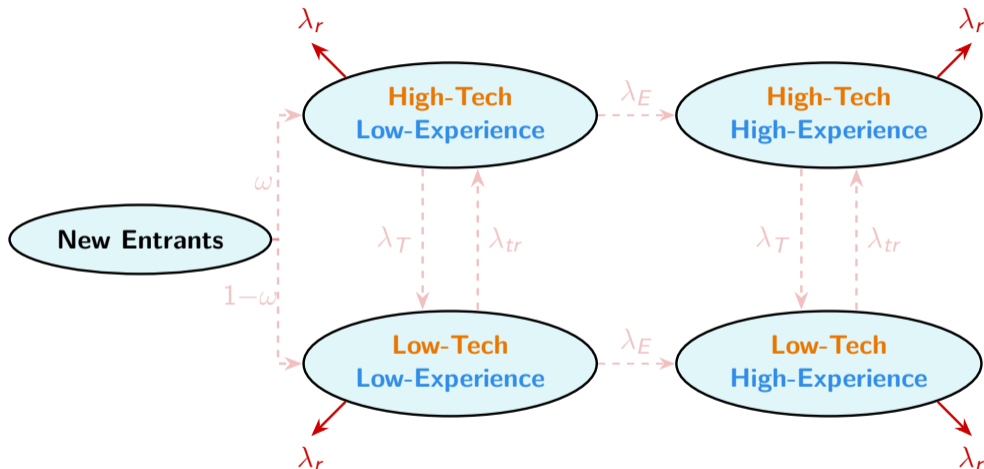
- Tech skills become obsolete at rate λ_T .

Workers: Skill Transitions



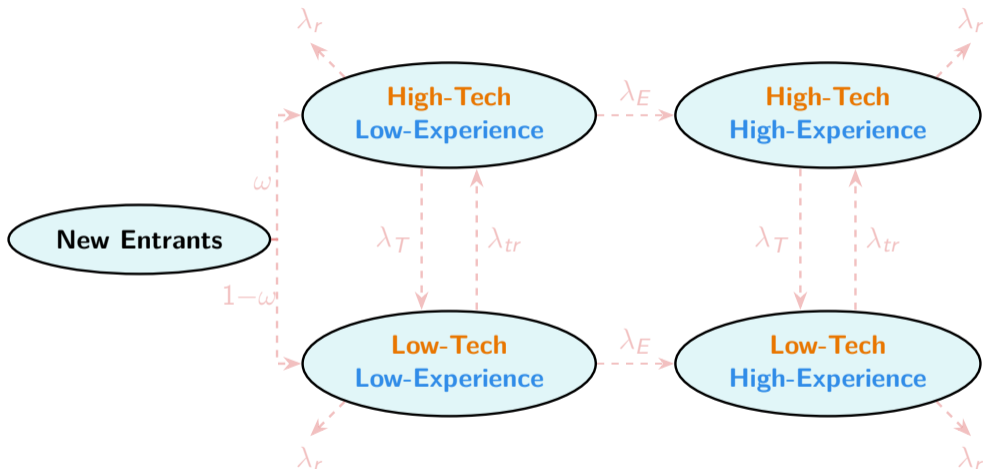
- Firms can retrain workers at rate λ_{tr} .

Workers: Skill Transitions



- ▶ Workers retire at rate λ_r .

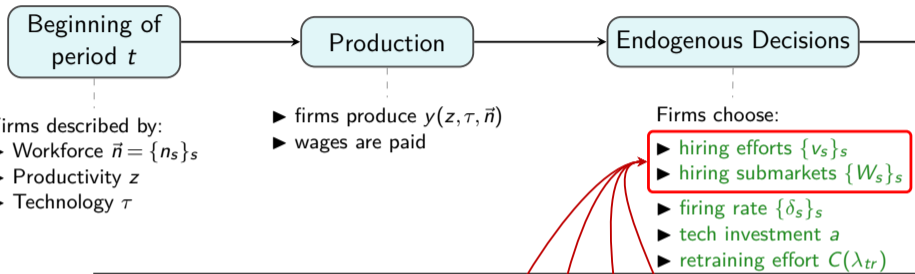
Workers: Skill Transitions



► Population \mathcal{L} evolves according to

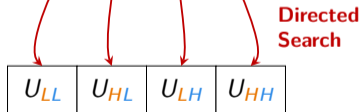
$$\underbrace{\mu_t}_{\text{New Entrants}} = \underbrace{\mathcal{L}_t}_{\text{Population growth rate}} \underbrace{g}_{\text{Population growth rate}} + \underbrace{\lambda_r \mathcal{L}_t}_{\text{Retirement}}$$

Timeline



One transition is realized:

- ▶ hiring $\{v_s \eta_s(W_s)\}_s$
- ▶ firms dissolution s_F ,
- ▶ worker separation $\{s_s^W, \delta_s\}_s, \lambda_r$
- ▶ tech change $\mathbb{P}(a)$
- ▶ skill change $\lambda_{tr}, \lambda_T, \lambda_P$
- ▶ productivity shock $F_z(z'|z)$



Production Technologies

► At any instant, two technologies are available:

- **Frontier** ($\tau = 0$) and **Laggard** ($\tau = 1$)

► The production function of technology τ is

$$y_\tau = \underbrace{z\lambda^{-\tau}}_{\text{TFP}} \underbrace{\left[\alpha_\tau L_T^\varphi + (1 - \alpha_\tau) L_E^\varphi \right]}_{\text{Labor Composite}}^{\frac{\eta}{\varphi}}, \quad \eta < 1$$

► **A1.** $\lambda > 1 \implies$ **Frontier** ($\tau=0$) have higher **TFP**.

► **A2.** $\alpha_0 > \alpha_1 \implies$ **Frontier** ($\tau=0$) are more **tech-skill intensive**.

Production Technologies

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► **Task Assignment.** Given a firm's workforce $\vec{n} = \{n_s\}_{s \in \mathcal{S}}$

$$L_T = \gamma_T^H \underbrace{\left(n_{HH}^T + n_{HL}^T \right)}_{\text{High}} + \gamma_T^L \underbrace{\left(n_{LL}^T + n_{LH}^T \right)}_{\text{Low}} \quad (\text{Tech-Skill})$$

$$L_E = \gamma_E^H \underbrace{\left(n_{HH}^E + n_{LH}^E \right)}_{\text{High}} + \gamma_E^L \underbrace{\left(n_{LL}^E + n_{HL}^E \right)}_{\text{Low}} \quad (\text{Experience})$$

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▶ **Technology Transitions.** Firms can invest $a \geq 0$ to affect the following

- **Tech-Upgrade.** **Laggard** become **Frontier** at rate $q_{10}(\underline{\mathbf{a}}_+)$
- **Tech-Downgrade.** **Frontier** become **Laggard** at rate $q_{01}(\underline{\mathbf{a}}_-)$
- **Obsolescence.** **Laggard** firms exit the market at rate $q_{12}(\underline{\mathbf{a}}_-)$

Firm Problem

► State Variables: $\vec{s} \equiv (z, \tau, \vec{n}, \vec{W}) = (z, \tau, \{n_i, W_i\}_{i \in \mathcal{S}})$, $\vec{n} \in \mathcal{N}_+^4$

► Hiring Process: firms post **one vacancy for each skill type** $i \in \mathcal{S}$

► **Dynamic contracts**

$$\mathcal{C}(s) = \left\{ \{w_i, v_i, \delta_i, W'_i(s_i^+)\}_{i \in \mathcal{S}}, \lambda_{tr}, a_\tau \right\}$$

subject to **promise keeping constraint** + **worker's participation constraint**.

► **Exogenous Shocks**

- Productivity Shocks: $F(z'|z)$
- Firm Dissolution: s^F
- Worker Separation: $s_i^W, \forall i \in \mathcal{S}$
- Skill obsolescence / experience: λ_T, λ_E
- Retirement: λ_r

Key Property of the Problem

- Define the **Joint Surplus**: $\Sigma(\vec{n}, z, \tau) \equiv \underbrace{J(\vec{s})}_{\text{Firm's Value}} + \sum_i n_i \underbrace{W_i}_{\text{Worker's Value}}$

Proposition (Schaal [2017])

Solving the firm's problem is equivalent to maximize to joint surplus:

$$c^\Sigma = \left\{ \left\{ \underbrace{v_i}_{\text{Recruitment}}, \underbrace{\delta_i}_{\text{Firing}}, \underbrace{W'_i(s_i^+)}_{\text{Continuation Promise}} \right\}_{i \in \mathcal{S}}, \underbrace{\lambda_{tr}}_{\text{Re-training}}, \underbrace{a_\tau}_{\text{Tech Investment}} \right\}$$

Key Result

- The joint surplus doesn't depend on promised utilities $\rightarrow s = (\vec{n}, z, \tau)$

Assumptions

Value Function

Workers' Continuation Promises

- ▶ Assume Cobb-Douglas matching function with matching elasticity γ ,

$$M(V, U) = V^\gamma U^{1-\gamma}.$$

- ▶ The worker's continuation promise is

$$W'_i(s_i^+) = \gamma \mathcal{U}_i + (1-\gamma) \underbrace{\left[\Sigma(s_i^+) - \Sigma(s) \right]}_{\text{Surplus Gain from Hiring}}, \quad \forall i \in \mathcal{S},$$

equivalent to Nash bargaining solution evaluated at the Hosios condition.

- ▶ Wages are pinned down by promise keeping constraint holding with equality.

BGP

A stationary equilibrium consists of **value functions** $J(s), W(s), \Sigma(s), \{w_i(s), v_i(s), \delta_i(s), W'_i(s)\}_{i \in \mathcal{S}}, \pi_e(s), a_\tau(s)$, **unemployment values** $\{U_i\}_{i \in \mathcal{S}}$, a **per-capita distribution** $\Lambda(s)$, **per-capita masses of active firms** F and **entrants** F_e , **per capita measures of employment and unemployment** per each type $\{E_i, U_i\}_{i \in \mathcal{S}}$, such that:

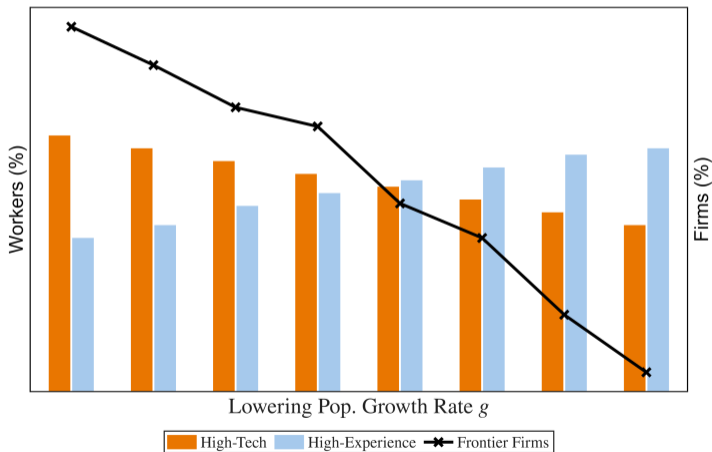
- ▶ ***Optimality holds.***
- ▶ ***Distributions and measures per capita are stationary.***
- ▶ ***Free-entry holds: $J^e = 0$***

Free Entry

Calibration Strategy

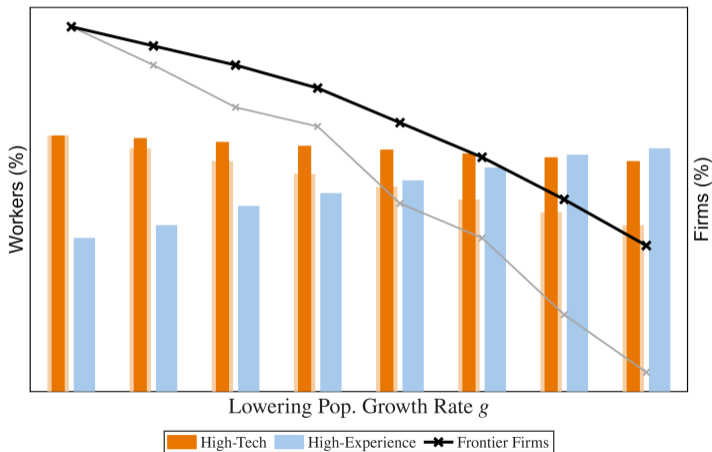
Aging, Skill Composition and Technology Adoption

- ▶ **Lowering g** \implies Experience \uparrow , Tech-Skills \downarrow , Frontier Adoption \downarrow .



Aging, Skill Composition and Technology Adoption

- ▶ **Low Training Cost** \implies Smoother Transition of Skills and Adoption.



Outline

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Aggregate Productivity

Aggregate Productivity: output per-worker (\mathcal{Y}/E).

Productivity Decomposition

$$\begin{aligned} \text{Productivity} &= \underbrace{(\text{Avg Size})^{1-\eta}}_{\text{DRS}} \times \text{Avg (Standardized) Output} = \\ &= (\text{Avg Size})^{1-\eta} \times \underbrace{\sum_{z,\tau} \text{Share}(z,\tau)}_{\text{Productivity Selection}} \times \text{Avg (Standardized) Output}(z,\tau) \\ &= (\text{Avg Size})^{1-\eta} \times \sum_{z,\tau} \text{Share}(z,\tau) \times \underbrace{\sum_n \sum_m \text{Output}(n,m)}_{\text{Scale Composition}} \times \underbrace{\text{Share}(m|n)}_{\text{Within-firm Misallocation}} \times \underbrace{\text{Share}(n)}_{\text{Between-firm Misallocation}} \end{aligned}$$

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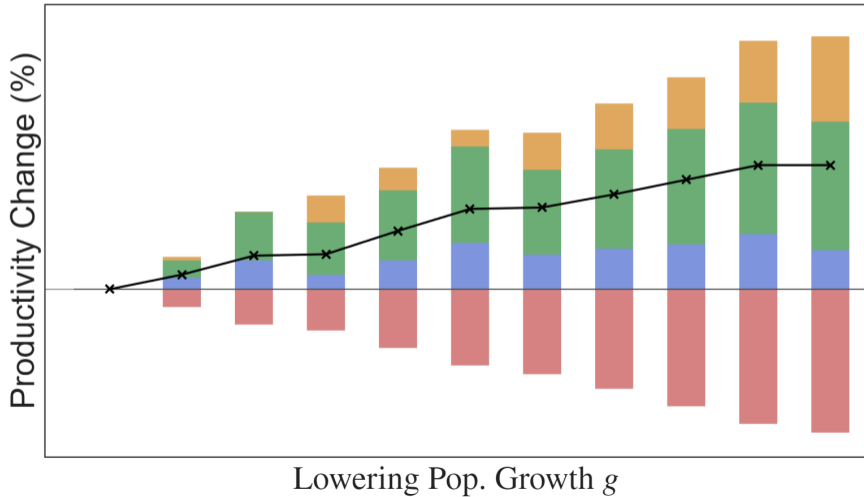
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Productivity Decomposition

► Low $g \implies \uparrow$ Loss from Productivity Selection.

Simulation



Conclusions and Next Steps

- ▶ Aging reshuffles the economy's skill mix: experience \uparrow , tech-skills \downarrow .
- ▶ Impact on aggregate productivity depends on the effect on tech adoption and labor misallocation.
- ▶ Construct a model that can separate various effects and suggest targeted policy interventions.
- ▶ **Next Steps:**
 - Calibrate the model using German data.
 - Feed projected future population aging path and study the effect on productivity.
 - Perform policy analysis: training cost \downarrow , firing costs \downarrow .

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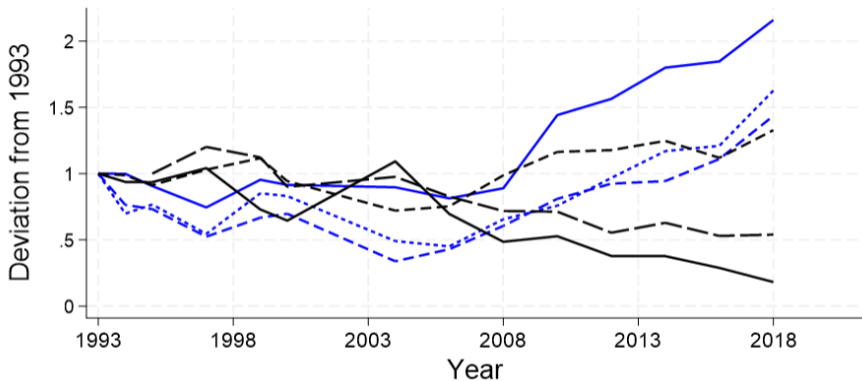
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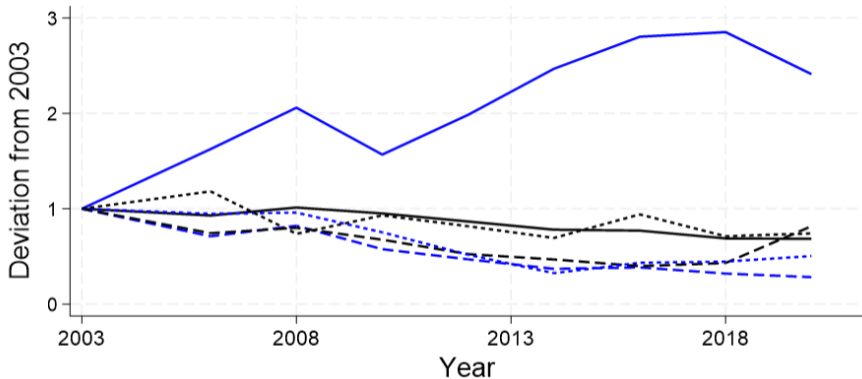
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Main Concerns About Staffing



- Aging Population
- Excessive Turnover
- Demand for Further Training
- Skill Shortage
- Overstaffing
- High Labor Cost

Main Constraints to Innovation

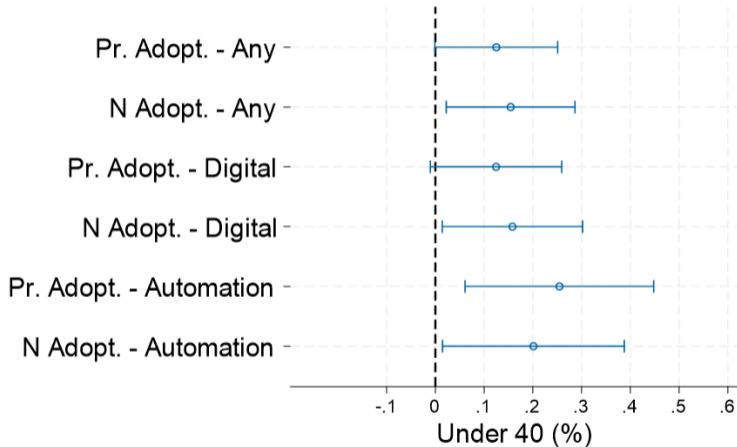


- Skill Shortage
- High Costs
- Customer Acceptance
- - - Lack Financing
- - - High Risk
- Law/Norms

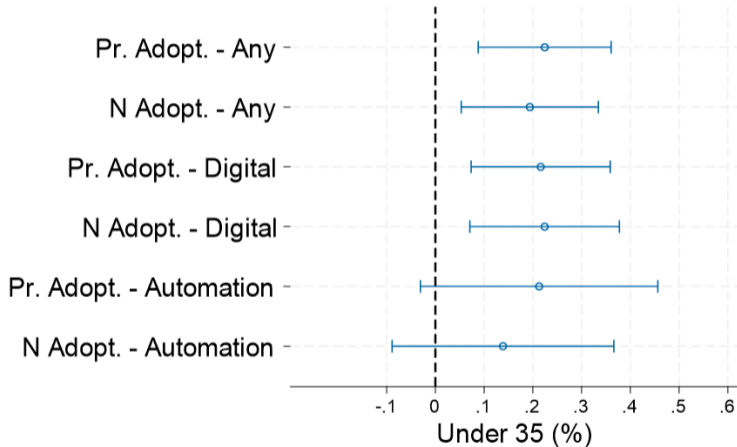
LPP-ADIAB Overview

- ▶ **Sample:** \approx 750 establishments per wave.
 - Representative of firms $>$ 50 employees.
 - Representative survey of employees are surveyed (7 per firm avg.)
- ▶ Advanced technologies surveyed
 - **Digital:** e.g., IoT, Big Data Analytics, AI, Virtual Reality.
 - **Automation:** e.g., Robots, Drones, Additive Manufacturing.
- ▶ Usage Options (for each tech.)
 - Use $<$ 2 years ago \rightarrow **Adoption Event** at $t - 2$.
 - Use $>$ 2 years ago \rightarrow **Control/Exclude**.
 - Not Use.

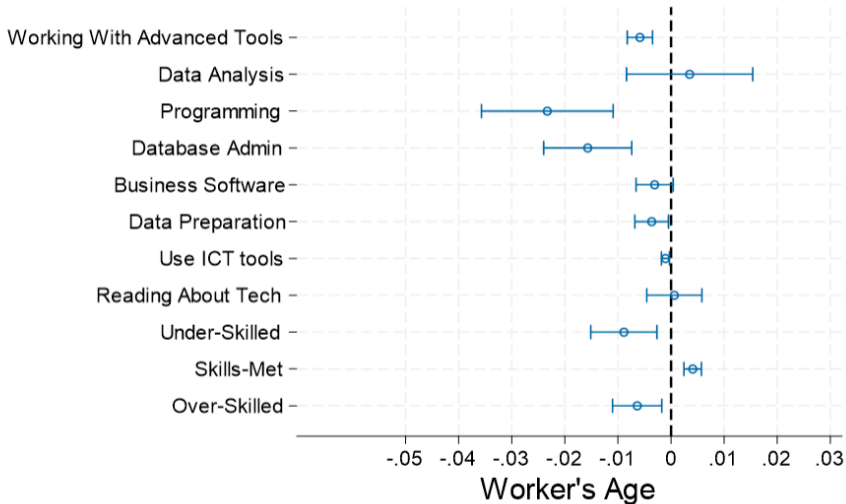
Young Workforce Predicts Higher Adoption



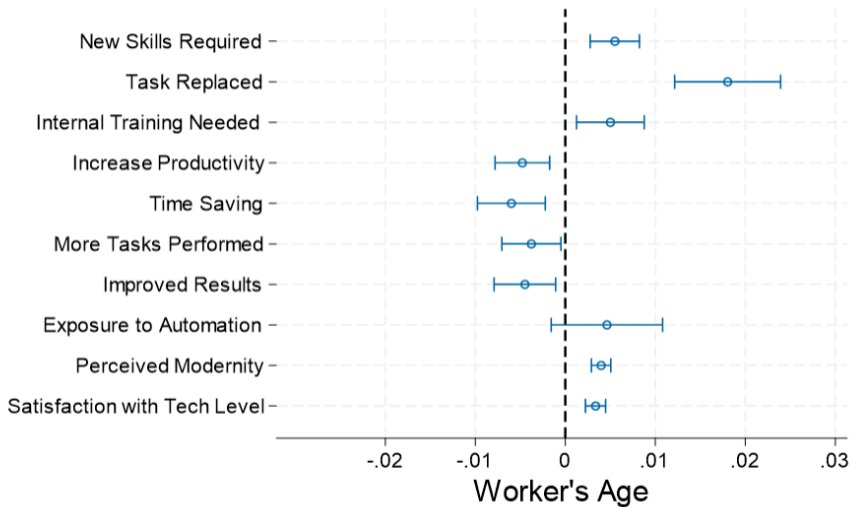
Young Workforce Predicts Higher Adoption



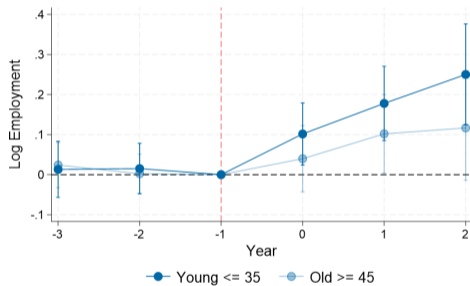
Young Perform More Tech-Related Tasks



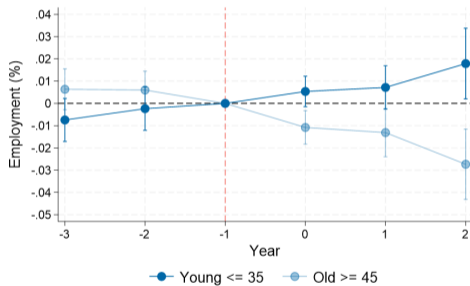
Young Report Productivity Gains for Tech Adoption



Event Study - Employment Share



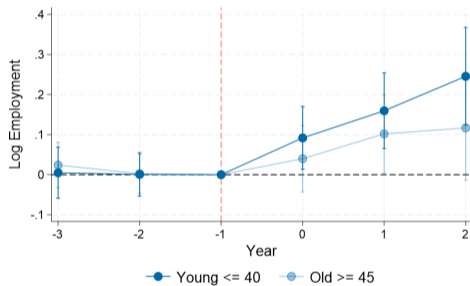
(a) Log Employment



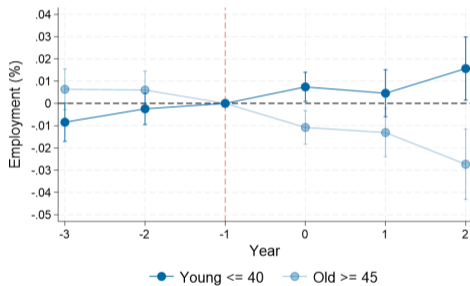
(b) Employment Share

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Event Study - Under 40



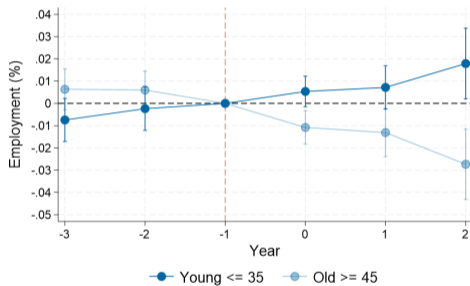
(a) Log Employment



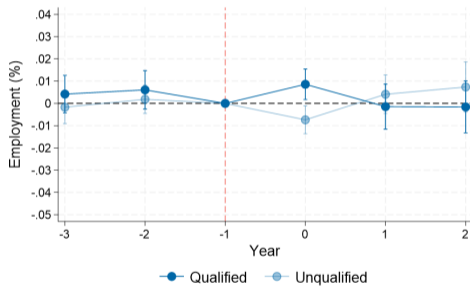
(b) Employment Share

[Back](#)

Event Study - College Heterogeneity



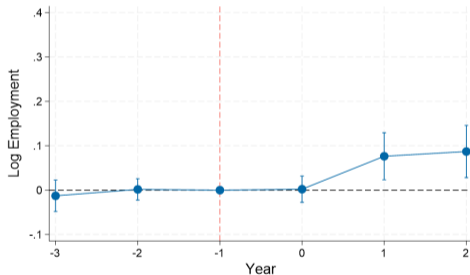
(a) Age Heterogeneity



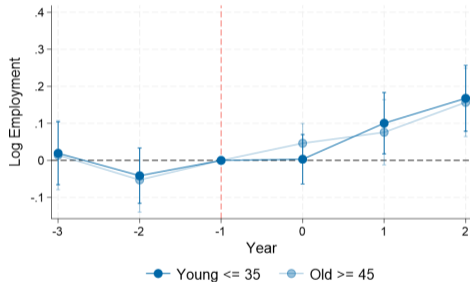
(b) College Heterogeneity

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Event Study - Automation Technologies



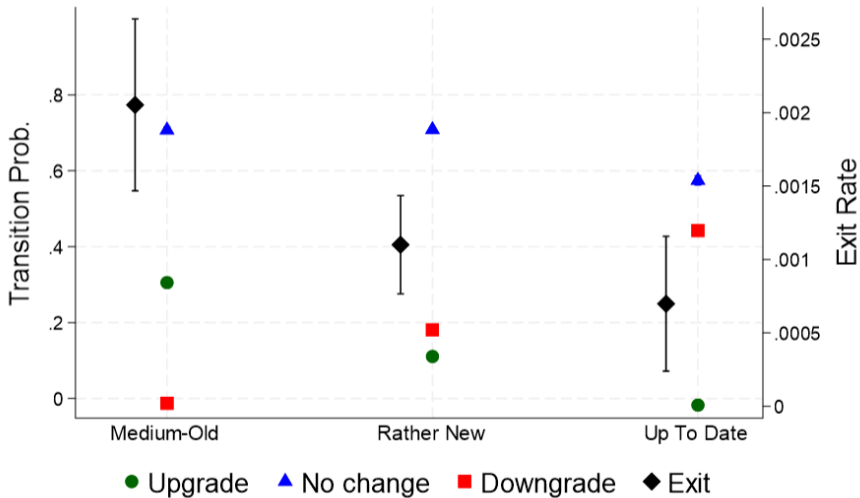
(a) Log Employment



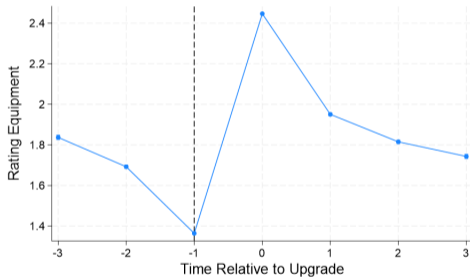
(b) Age Heterogeneity

[Back](#)

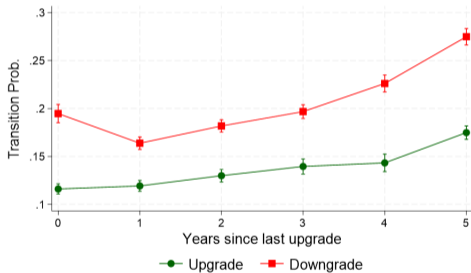
Tech Transition in the Data



Cyclicity of Tech Upgrade



(a) Equipment Rating

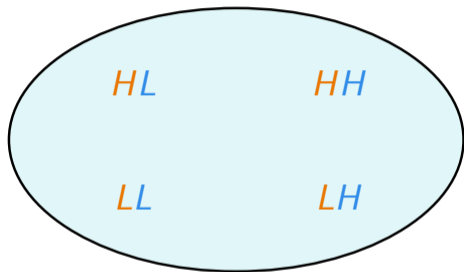


(b) Upgrade - Downgrade

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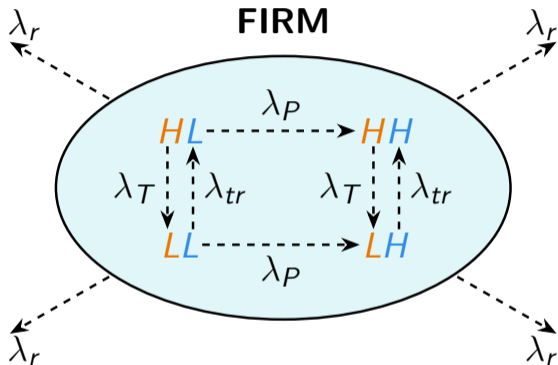
Firms' Workforce

FIRM



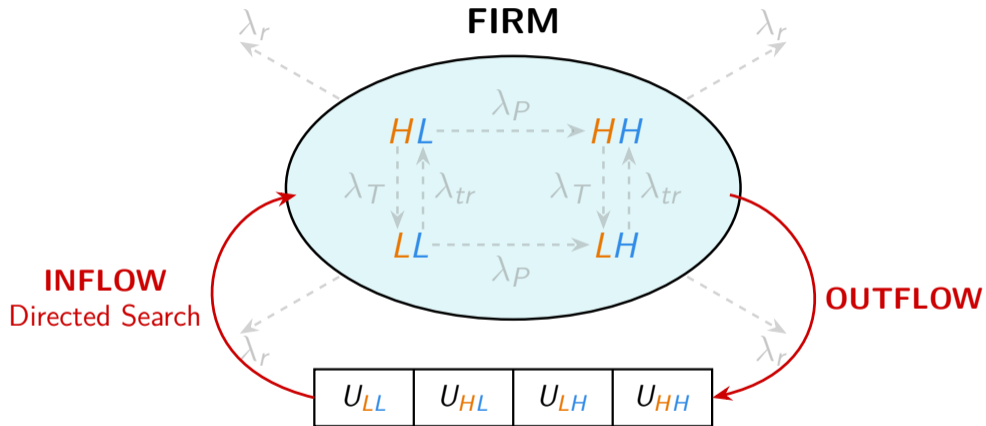
- ▶ A firm is a collection of workers of different types.

Firms' Workforce



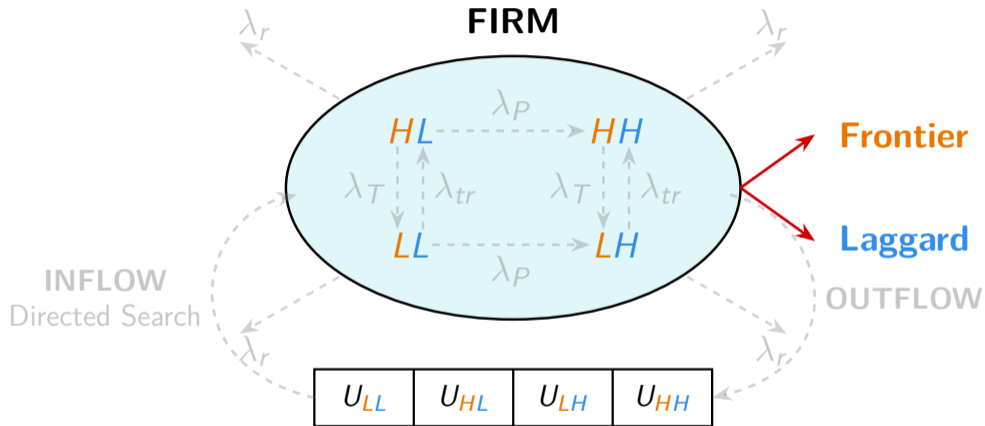
- **Workers transitions:** obsolescence, experience, up-skilling, retirement.

Firms' Workforce



- ▶ **Inflows:** type-specific hiring from unemployment.
- ▶ **Outflows:** Endogenous + Exogenous separations.

Firms' Workforce



- **Technology Choice:** skill-mix of incumbents + availability of skills from U

Unemployed Workers

The value of an unemployed worker of type $i \in \mathcal{S}$ is

$$(\rho + \lambda^r) \mathcal{U}_i = \max_W \left\{ b + \underbrace{\mu_i(W)}_{\text{Job Finding Rate}} \max\{W - \mathcal{U}_i, 0\} + \underbrace{\lambda_T(\mathcal{U}_{L,SP} - \mathcal{U}_{H,SP})}_{\text{Tech Obsolescence}} \underbrace{\mathbb{1}\{s_T = H\}}_{\text{High-tech Worker}} \right\}$$

$$\implies \mu_i(W) = \frac{(\rho + \lambda^r) \mathcal{U}_i - b - \lambda_T(\mathcal{U}_{L,SP} - \mathcal{U}_{H,SP}) \mathbb{1}\{s_T = H\}}{W - \mathcal{U}_i}, \quad s_P \in \{L, H\}$$

Trade-off: job-finding rate is **inversely related** to the contract's promised value W

- ▶ $W \uparrow \implies$ submarket (i, W) attracts more workers $\implies \mu_i(W) \downarrow$, wait time \uparrow
- ▶ Continuum of active submarkets maximizing unemployment value.

Potential Entrants

- ▶ Potential entrants' value:

$$J^e = \underbrace{-\kappa}_{\text{Entry Cost}} + \underbrace{p_0 \tilde{J}^e(\tau=0) + (1-p_0) \tilde{J}^e(\tau=1)}_{\text{Expected Profits}}$$

- Pay a flow cost to open a business: κ
- Enter as frontier with probability p_0 .

- ▶ Upon entry:

$$\tilde{J}^e(\tau) = \sum_z F^e(z) \left[\max_{\{W'_i\}} \sum_{i \in \mathcal{S}} \eta_i (W'_i(s_i^e)) J(s_i^e) \right], \forall i$$

- Draw a **random productivity shock** from F_z^e
- **Post one vacancy** for each type of worker, choosing the submarket W_i .

Key Property of the Problem

► Assume:

1. Utilities are linear and transferrable across agents
2. Contract space is complete: state-contingent contracts
3. Directed search

► Define the **Joint Surplus**: $\Sigma(\vec{n}, z, \tau) \equiv \underbrace{J(\vec{s})}_{\text{Firm's Value}} + \sum_i n_i \underbrace{W_i}_{\text{Worker's Value}}$

Proposition (Schaal [2017])

Solving the firm's problem is equivalent to maximize to joint surplus over the simpler contract space:

$$\mathcal{C}^\Sigma = \left\{ \left\{ \underbrace{v_i}_{\text{Recruitment}}, \underbrace{\delta_i}_{\text{Firing}}, \underbrace{W_i'(s_i^+)}_{\text{Continuation Promise}} \right\}_{i \in \mathcal{S}}, \underbrace{\pi_e}_{\text{Re-training}}, \underbrace{a_\tau}_{\text{Tech Investment}} \right\}$$

The joint surplus doesn't depend on promised utilities: new state space: $s = (\vec{n}, z, \tau)$

Notation: Evolution of State Variables

Back

Remark: Given continuous time, only one state transition can happen simultaneously.

$$\vec{s}' \equiv (\vec{n}, z', \tau') \in \left\{ \begin{array}{ll} (n_{LL} + 1, \vec{s}_-), (n_{LH} + 1, \vec{s}_-), (n_{HL} + 1, \vec{s}_-), (n_{HH} + 1, \vec{s}_-) & \text{Hiring } i: \vec{s}_i^+, \forall i \\ (n_{LL} - 1, \vec{s}_-), (n_{LH} - 1, \vec{s}_-), (n_{HL} - 1, \vec{s}_-), (n_{HH} - 1, \vec{s}_-) & \text{Firing } i: \vec{s}_i^-, \forall i \\ (n_{LL} - 1, n_{HL} + 1, \vec{s}_-), (n_{LH} - 1, n_{HH} + 1, \vec{s}_-) & \text{Up-skilling: } \vec{s}_{\pi_e} \\ (n_{HL} - 1, n_{LL} + 1, \vec{s}_-), (n_{HH} - 1, n_{LH} + 1, \vec{s}_-) & \text{Obsolescence: } \vec{s}_{\lambda_T} \\ (n_{LL} - 1, n_{LH} + 1, \vec{s}_-), (n_{HL} - 1, n_{HH} + 1, \vec{s}_-) & \text{Experience: } \vec{s}_{\lambda_R} \\ (n_{LL} - 1, \vec{s}_-), (n_{LH} - 1, \vec{s}_-), (n_{HL} - 1, \vec{s}_-), (n_{HH} - 1, \vec{s}_-) & \text{Retirement: } \vec{s}_{\lambda_o} \\ (\tau', \vec{s}_-) & \text{Tech Change: } \vec{s}_{\tau'} \\ (z', \vec{s}_-) & \text{Prod. Shock: } \vec{s}_{z'} \end{array} \right.$$

Firm's Problem

Back

► Long-Term Contract: $\vec{c} = \left\{ \{w_i, v_i, \delta_i, W'_i(\vec{s})'\}_{i \in \{LL, LH, HL, HH\}}, \pi_e, a_\tau \right\}$

$$\rho J(\vec{s}) = \max_{\vec{c}} \left\{ y - C_e(\pi_e)(n_{LL} + n_{LH}) - C_\tau(a_\tau) + s^F (J^e - J(\vec{s})) \right.$$

Workforce Costs $-\sum_i \left[w_i n_i + C_{\delta_i}(\delta_i) n_i + C_{v_i}(v_i) \right]$

Hiring $+ \sum_i v_i \eta_i (W'_i(\vec{s}_i^+)) (J(\vec{s}_i^+) - J(\vec{s})) \left. \right\}$

Separations $+ \sum_i (\delta_i + s_i^W) n_i (J(\vec{s}_i^-) - J(\vec{s})) + \sum_i \lambda_r n_i (J(\vec{s}_{\lambda_o}) - J(\vec{s}))$

Skill Change $+ \sum_{i \in \{LL, LH\}} \pi_e (J(\vec{s}_{\pi_e}) - J(\vec{s})) + \sum_{i \in \{HL, HH\}} \lambda_T (J(\vec{s}_{\lambda_T}) - J(\vec{s})) + \sum_{i \in \{LL, HL\}} \lambda_P (J(\vec{s}_{\lambda_P}) - J(\vec{s}))$

Tech Change $+ \sum_{\tau'} \pi(\tau' | \tau, a) (J(\vec{s}_{\tau'}) - J(\vec{s}))$

Prod. Shock $+ \sum_{z'} F_z(z' | z) (J(\vec{s}_{z'}) - J(\vec{s})) \left. \right\} \quad \text{s.t.} \quad W_i(\vec{c}) \geq W_i, \quad W'_i \geq U_i, \quad \forall i$

Joint Surplus Maximization

Back

$$(\rho + s^F)\Sigma(s) = \max_{\mathcal{C}^\Sigma} \left\{ y - C_e(\pi_e)(n_{LL} + n_{LH}) - C_\tau(a_\tau) - \sum_i \left[C_{\delta_i}(\delta_i)n_i + C_{v_i}(v_i) \right] \right\}$$

$$\text{Outside Option} \quad + \sum_i n_i (\delta_i + s_i^W + s^F) \mathcal{U}_i$$

$$\text{Utility to New Hires} \quad - \sum_i v_i \eta_i (W'_i(s_i^+)) W'_i(s_i^+)$$

$$\text{Hiring} \quad + \sum_i v_i \eta_i (W'_i(s_i^+)) (\Sigma(s_i^+) - \Sigma(s))$$

$$\text{Separations} \quad + \sum_i (\delta_i + s_i^W) n_i (\Sigma(s_i^-) - \Sigma(s)) + \sum_i \lambda_r n_i (\Sigma(\vec{s}_{\lambda_r}) - \Sigma(\vec{s}))$$

$$\text{Skill Change} \quad + \sum_{i \in \{LL, LH\}} \pi_e (\Sigma(\vec{s}_{\pi_e}) - \Sigma(\vec{s})) + \sum_{i \in \{HL, HH\}} \lambda_T (\Sigma(\vec{s}_{\lambda_T}) - \Sigma(\vec{s})) + \sum_{i \in \{LL, HL\}} \lambda_P (\Sigma(\vec{s}_{\lambda_P}) - \Sigma(\vec{s}))$$

$$\text{Tech Change} \quad + \sum_{\tau'} \pi(\tau' | \tau, a_\tau) (\Sigma(s_{\tau'}) - \Sigma(s))$$

$$\text{Prod. Shock} \quad + \sum_{z'} F_z(z' | z) (\Sigma(s_{z'}) - J(s)) \left. \right\}$$

Joint Surplus Maximization

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$$(\rho + s^F)\Sigma(s) = \max_{\mathcal{C}^\Sigma} \left\{ y - C_e(\pi_e)(n_{LL} + n_{LH}) - C_\tau(a_\tau) - \sum_i \left[C_{\delta_i}(\delta_i)n_i + C_{v_i}(v_i) \right] \right.$$

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$$\text{Tech Change} \quad + \sum_{\tau'} \pi(\tau' | \tau, a_\tau) (\Sigma(s_{\tau'}) - \Sigma(s))$$

$$\text{Prod. Shock} \quad + \sum_{z'} F_z(z' | z) (\Sigma(s_{z'}) - J(s)) \left. \right\}$$

Joint Surplus Maximization

Back

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Outside Option $+ \sum_i n_i (\delta_i + s_i^W + s^F) \mathcal{U}_i$

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Prod. Shock $+ \sum_{z'} F_z(z' | z) (\Sigma(s_{z'}) - J(s)) \}$

Joint Surplus Maximization

Back

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Joint Surplus Maximization

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Joint Surplus Maximization

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Joint Surplus Maximization

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Tech Change $+ \sum_{\tau'} \pi(\tau' | \tau, a_\tau) (\Sigma(s_{\tau'}) - \Sigma(s))$

Prod. Shock $+ \sum_{z'} F_z(z' | z) (\Sigma(s_{z'}) - J(s)) \}$

Aggregate productivity

$$\begin{aligned}
 \frac{\mathcal{Y}}{E} &= \frac{1}{E} \sum_{s \in \mathcal{S}} y^*(s) f(s) \\
 &= \frac{F}{E} \sum_{z, \tau} \frac{F_{z, \tau}}{F} \sum_n y^*(s) \tilde{f}_{z, \tau}(n) \\
 &= \underbrace{\left(\frac{F}{E} \right)^{1-\nu}}_{\text{Firm Size}} \sum_{z, \tau} \underbrace{\frac{F_{z, \tau}}{F}}_{\text{Firm Selection}} \underbrace{\sum_{\hat{n}, m} y_{z, \tau}^*(\hat{n}, m) g_{z, \tau}(\hat{n}, m)}_{\text{Workers Allocation}}
 \end{aligned} \tag{1}$$

where

$$g_{z, \tau}(\hat{n}, m) = \sum_n \tilde{f}_{z, \tau}(n) \mathbb{I} \left\{ \frac{n}{E/F} = \hat{n} \ \& \ m_\tau = m \right\}$$

Calibration Strategy

▶ New Entrant Workers

- **Model:** HL w.p. ω ; LL w.p. $1 - \omega$.
- **Data:** HL if college (C); LL otherwise (NC).

▶ Exog. Skill Transitions: $\lambda_T, \lambda_E \implies$ Life-Cycle Wage Profiles.

- **High λ_E :** Faster early growth for NC + Flattening earlier in life.
- **High λ_T :** Slower early growth for C + Faster decrease of college premium.

▶ Endog. Skill Transitions: λ_{tr}

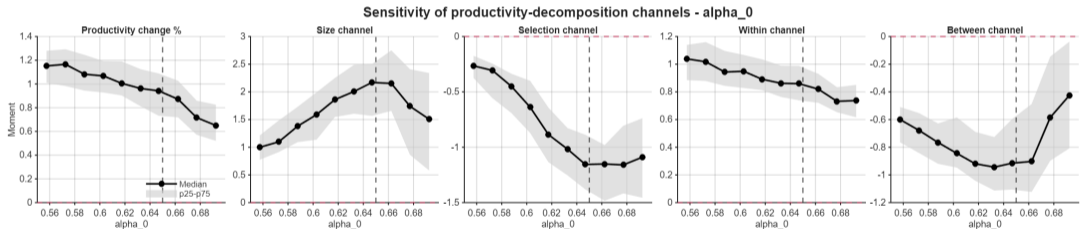
- Calibrate the **cost of training** to info on on-the-job training participation within firms.

Calibration Strategy

- ▶ Skill Complementarity: φ
 - Correlation between within firm wage-dispersion and age dispersion.
- ▶ Task weights: α_T
 - Match event study regressions upon adoption.
- ▶ Efficiency Units: $\gamma_T^H, \gamma_T^L, \gamma_E^L$
 - **High** $\frac{\gamma_T^H}{\gamma_T^L}$: Larger Wage dispersion early in life.
 - **High** $\frac{\gamma_E^H}{\gamma_E^L}$: Higher Level growth of NC.
 - **High** $\frac{\gamma_E^H}{\gamma_T^H}$: Higher Level growth of C.

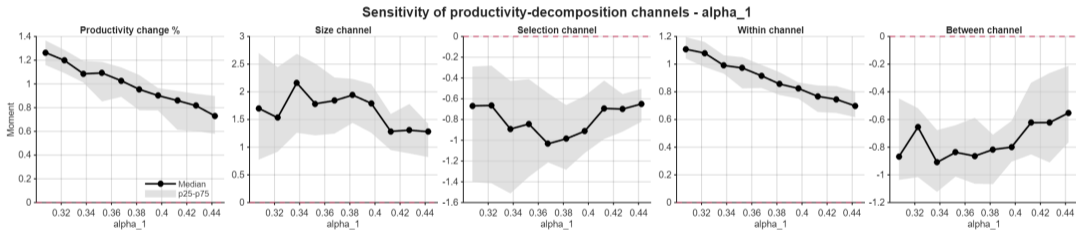
Simulation of Productivity Decomposition: α_0

- ▶ α_0 : Weight of Tech-Skills in Frontier Production.



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Simulation of Productivity Decomposition: α_1



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Aging, Skill Composition and Technology Adoption

- ▶ Low Training Cost + **Skill Substitutes** \implies Very Little Effect.

